## 1984 Q1

The driver of a car travelling at 20m/s sees a second car 120m in front, travelling in the same direction at a uniform speed of 8m/s.

- (a) What is the least retardation that must be applied to the faster car so as to avoid a collision? (0.6)
- (b) If the actual retardation is 1m/s<sup>2</sup>, calculate
  - (i) the time interval, in seconds, for the faster car to reach a point 66m behind the slower (6s)
  - (ii) the shortest distance between the cars. (48m)

## 1984 Q2

A ship B is travelling in a direction  $41^0$  East of North at 15m/s. A second ship C is travelling  $41^0$  South of East at 20m/s. Calculate

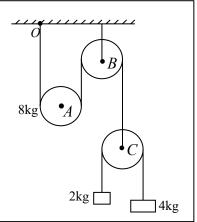
- (i) the velocity of B relative to C
- (ii) the shortest distance between the ships if C is 3km east of B at a particular moment;
- (iii) the time interval during which the ships remain in visual contact, if visibility is limited to 3km

A plane is inclined at an angle  $\tan^{-1}(\frac{1}{2})$  to the horizontal. A particle is projected up the plane with velocity u at an angle  $\theta$  to the plane. (The plane of projection is vertical and contains the line of greatest slope.) The particle strikes the plane parallel to the horizontal.

Express t, the time of flight, in terms of u and  $\theta$ . Hence, or otherwise, establish that  $\tan \theta = 1/3$ . Calculate the range along the plane.

The diagram shows a light inextensible string having one end fixed at O, passing under a movable pulley A of mass 8kg and then over a fixed light pulley B. The other end of the string is attached to a light pulley C, of negligible mass. Over pulley C, a second light inextensible string is passed having particles of mass 2 and 4 kg respectively, attached. All pulleys are smooth.

- (i) Show in a diagram the forces acting on each pulley when the system is released from rest.
- (ii) Find the acceleration of pulley A, pulley C, each particle.



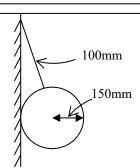
- (a) A smooth sphere of mass 3kg and velocity  $u_1$  collides directly with another smooth sphere of mass 4kg and velocity  $u_2$  both moving in the same direction. Show that  $7v_1 = u_1(3 - 4e) + 4u_2(1 + e)$  where  $v_1$  is the velocity of the 3kg sphere after the collision. Hence, show that the impulse which each sphere receives is  $\frac{12}{7}(1 + e)(u_2 - u_1)$ .
- (b) A smooth sphere of mass 4kg collides with another smooth sphere of mass m which is at rest. After impact the two spheres move at right angles to each other. If the coefficient of restitution was  $\frac{4}{7}$ , calculate the value of m.

- (a) A particle moving on the inside smooth surface of a fixed hollow sphere of internal radius  $\sqrt{2}$  m describes a horizontal circle of radius 1m. Calculate the angular velocity of the particle.
- (b) Two particles of equal mass attached by a taut inextensible string of length 2y rests on a horizontal circular table. The particles are respectively y and 3y from the centre of the table so that centre and particles are collinear. The table rotates about its centre with angular velocity  $\mathbf{w}$  and the coefficient of friction is  $\frac{y}{2}$ .

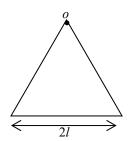
If both particles are on the point of slipping,

- (i) show on a diagram, all the forces of the string/particle system
- (ii) calculate w.
- (a) A sphere of mass 3kg and radius 150mm is suspended by a string 100mm long, the string joining a point on the surface with a point on a smooth vertical wall.

Find the tension in the string in terms of g.



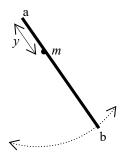
(b) A heavy uniform rod of mass m and length 2l is suspended from a point, o, by two equal inelastic strings. Each string is fixed to o and to an end point of the rod so that the rod hangs horizontally. If, then, a mass m/2 is suspended half-way between the centre and one end of the rod so that the rod is no longer horizontal, calculate the ratio  $T_1:T_2$ , where  $T_1$  is the tension in one of the strings and  $T_2$ , the tension in the other.



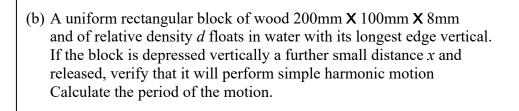
A uniform rod [ab] of length 2p and of mass 3m has a mass m attached to it at a distance y from a. Prove that the moment of inertia of this system about a smooth horizontal axis through a is  $4mp^2 + my^2$ .

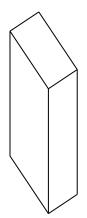
The system oscillates in a vertical plane about a. If the length of the equivalent simple pendulum is  $\frac{40}{33}p$ ,

show that y is either  $\frac{2}{3}p$  or  $\frac{6}{11}p$ .



- (a) A body of mass 1.5kg weighs 2.1N in water and 3.36N in a mixture of another liquid A and water. If there was no reduction in volume when the mixture was made, calculate
  - (i) the relative density of the body
  - (ii) the relative density of the mixture
  - (iii) the volume of liquid *A*, of relative density 0.82, which must be added to 100ml of water to form the mixture.





- (a) Find the general solution to  $\frac{dv}{dt} = g kv$  where g and k are constants. Show that  $\frac{Lim\ v}{t \to \infty} = \frac{g}{k}$
- (b) A car, free-wheeling on a straight road, experiences a retardation which is proportional to the square of its speed. Its speed is reduced from 20m/s to 10m/s in a distance of 100m. Calculate the time taken to travel the 100m.