

## 1988 Q1

- (a) A particle moving in a straight line with uniform acceleration describes 23m in the fifth second of its motion and 31m in the seventh second. Calculate its initial velocity. **(5m/s)**
- (b) A particle falls from rest from a point  $o$ , passing three points  $a$ ,  $b$ , and  $c$ , the distances  $ab$  and  $bc$  being equal. If the particle takes 3 seconds to pass from  $a$  to  $b$  and 2 seconds from  $b$  to  $c$ , calculate  $|ab|$ . **(147m)**

## 1988 Q2

- (a) Two boats move with constant speed 5m/s relative to the water and both cross a straight river of width 72m flowing with constant speed 3m/s parallel to the banks. One crosses by the shortest path and the other in the shortest time. Show that the difference in the times taken is 3.6s.
- (b) Two ships  $A$  and  $B$  move with constant speeds  $2u$  and  $u$  respectively. At a certain instant,  $B$  is 2400m due east of  $A$  and moving northwards. Show that  $A$  must move in the direction  $30^\circ$  North of East in order to intercept  $B$  and find (in terms of  $u$ ) the time it takes to intercept  $B$ .

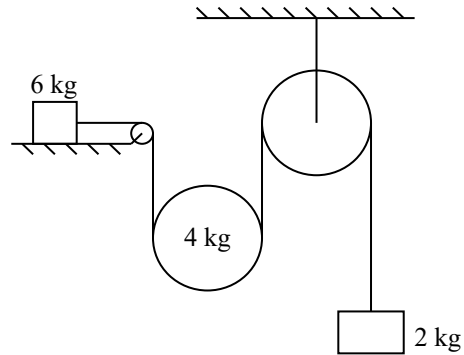
## 1988 Q3

- (a) A particle which is projected with speed  $u$  has a horizontal range  $\frac{3u^2}{49}$ . Calculate the two possible angles of projection.
- (b) A particle is projected up an inclined plane with initial speed  $13u$ . The line of projection makes an angle  $\tan^{-1}\left(\frac{5}{12}\right)$  with the plane and the plane is inclined at  $45^\circ$  to the horizontal. (The plane of projection is vertical and contains the line of greatest slope.) The particle strikes the plane at a point  $p$ . If the coefficient of restitution between the particle and the plane is 0.4, show that the particle rises vertically from  $p$  and strikes  $p$  again on the second bounce.

## 1988 Q4

One end of a light inextensible string is attached to a mass of 6 kg which rests on a rough horizontal table. The coefficient of friction between the mass and the table is  $\frac{1}{6}$ .

The string passes over a smooth fixed pulley at the edge. Then it passes under a smooth movable pulley of mass 4 kg and over a smooth fixed pulley. A mass of 2 kg is attached to its other end.

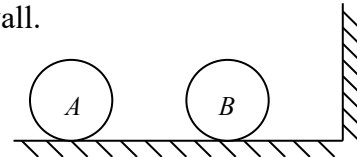


- Show on separate diagrams the forces acting on each mass.
- Calculate the acceleration of each mass and the tension in the string in terms of  $g$ , the acceleration due to gravity.

## 1988 Q5

Two smooth spheres  $A$  and  $B$ , of equal radii, have masses 4 kg and 8 kg respectively. They lie at rest on a smooth horizontal floor so that the line joining their centres is perpendicular to the vertical wall.  $A$  is projected towards  $B$  with speed  $u$  and collides with  $B$ .  $B$  then hits the wall, rebounds and collides with  $A$  again. This final collision reduces  $B$  to rest. If the coefficient of restitution between  $A$  and  $B$  is  $\frac{1}{4}$ , calculate

- the coefficient of restitution between  $B$  and the wall.
- the final velocity of  $A$  in terms of  $u$ .
- the total loss of energy due to the three collisions.



## 1988 Q6

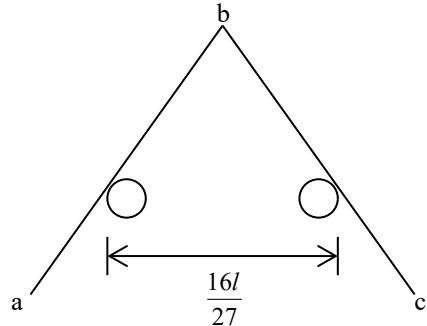
A particle of mass 8 kg is describing a circle, with constant speed  $v$ , on a smooth horizontal table. It is connected by a light inextensible string of length 3 m to a point which is 1 m vertically above the centre of the circle.

- Calculate the tension in the string.
- Show that the particle will remain in contact with the table if  $v < \sqrt{8g}$
- If the speed of the particle is increased to  $\sqrt{9.1g}$ , calculate the height at which the particle rotates above the table.

## 1988 Q7

Two equal uniform rods  $ab$  and  $bc$  each of length  $2l$  and weight  $W$ , are freely joined at  $b$  and rest in equilibrium, in a vertical plane, across two smooth horizontal pegs at the same horizontal level and distant  $\frac{16l}{27}$  apart.

- (i) Show in separate diagrams the forces acting on each rod.
- (ii) Show that the inclination of each rod to the vertical is  $\text{Sin}^{-1}\left(\frac{2}{3}\right)$ .
- (iii) Determine the magnitude and direction of the reaction at  $b$ .



## 1988 Q8

Show that the moment of inertia of a uniform rod of mass  $m$ , and length  $2l$ , about an axis through its centre of mass perpendicular to the rod is  $\frac{1}{3}ml^2$ .

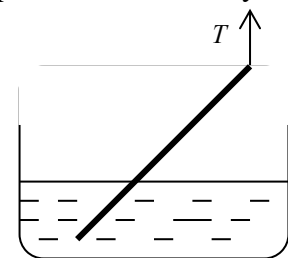
Three of these rods are joined together at their ends to form a triangle  $abc$ . The triangle is free to rotate about a fixed horizontal axis through  $a$ , perpendicular to its plane. Find the period of small oscillations about the equilibrium position.

## 1988 Q9

State the Principle of Archimedes.

A uniform rod of weight  $W$  and length  $2l$ , in equilibrium, is supported at one end by a vertical force  $T$  and is immersed in water as shown in the diagram. The relative density of the rod is  $\frac{7}{16}$ .

- (i) Calculate the length of the immersed part of the rod.
- (ii) Show that  $T = \frac{3w}{7}$ .



## 1988 Q10

(a) Solve the differential equation  $\frac{dx}{dt} = \sqrt{100 - 4x^2}$  if  $x = 5$  when  $t = 0$ .

(b) A particle of mass  $m$  is projected vertically upwards with speed 120 m/s in a medium where there is a resistance of  $0.098v^2$  per unit mass of the particle when  $v$  is the speed. Calculate the time taken to reach the highest point.